

## Full Length Article

# Reduced kinetics of NH<sub>3</sub>/n-heptane: Model analysis and a new small mechanism for engine applications

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## ABSTRACT

A compact reduced mechanism covering a wide range of conditions is developed for use in simulations of NH<sub>3</sub>/n-heptane combustion in engines. Reduction targets were selected after reviewing available experimental studies of NH<sub>3</sub> combustion in engines. Ignition, flames and oxidation of NH<sub>3</sub>/n-heptane mixtures were targeted. Particularly, mixtures with very low molar percentage of n-heptane which are important for the applications were considered. They have been observed to have a distinct ignition behavior. Target quantities also included pollutants with a goal to account for two possible mechanisms of N<sub>2</sub>O formation in engines, discussed in literature. The reduced mechanism of this study was developed with ant colony reduction method. It consists of 57 species and 159 reactions, and its range of applicability is 10–100 atm pressure and 0–100 % NH<sub>3</sub> in the fuel mixture. The performance of the mechanism was found comparable to larger models from literature. Importance of carbon–nitrogen interactions, influence of key reactions in the NH<sub>3</sub> subset and effect of CO on N<sub>2</sub>O formation were analyzed and discussed in terms of the predictive ability of the reduced mechanism of the present study and those available from literature.

## 1. Introduction

In recent years ammonia (NH<sub>3</sub>) has become widely considered as a potential fossil free energy carrier, suitable for energy storage and power generation [1]. In combustion research NH<sub>3</sub> was previously seen mainly as an intermediate in combustion of fuels with bound nitrogen [2], but now the research focus is shifting towards the use of NH<sub>3</sub> as a standalone fuel or in mixtures with other fuels. Different aspects related to the use of NH<sub>3</sub> as fuel in internal combustion engines (IC engines) and gas turbines have been reviewed in [3,4]. While early research focused mainly at the very possibility of a successful operation of an IC engine with NH<sub>3</sub>, since about 2020, a number of studies have explored NH<sub>3</sub> combustion over a broad range of parameters and examined their effect on engine efficiency and pollutant formation. Aspects studied are, for example, engine load, type and amount of the pilot fuel, and injection strategy. Table 1 presents a comparative overview of these studies.

Due to slow ignition of NH<sub>3</sub>, running an IC engine on neat NH<sub>3</sub> is challenging, but there exist some recent successful demonstrations [5,6], which implement spark-assisted compression ignition [5] or pre-chamber turbulent jet ignition [6]. The majority of other recent works implemented a dual-fuel strategy with various secondary fuels:

hydrogen [7–10], natural gas [11–13], dimethyl ether (DME) [14,15], n-heptane [16], diesel [17–25] or biodiesel [26], gasoline [27,28], or several of these [29].

In most studies, NH<sub>3</sub> is premixed with air at intake, however, direct injection of NH<sub>3</sub> has been applied by Ryu et al. [27] in a spark-ignition (SI) engine; and in compression-ignition (CI) engines by Kong and co-workers [14,15] who mixed liquid DME and NH<sub>3</sub> before injection, and by Zhang et al. [21] who used two injectors for NH<sub>3</sub> and diesel, respectively.

The amount of NH<sub>3</sub> in the fuel varies greatly in the studies outlined in Table 1. NH<sub>3</sub> content is commonly expressed as NH<sub>3</sub> energy fraction,  $X_{NH_3}^E$ . About half of the studies considered NH<sub>3</sub> to be primarily a fuel additive, with  $X_{NH_3}^E \leq 0.5$ . A few authors, however, achieved very high values of  $X_{NH_3}^E$ , in Table 1 listed as energy %: up to 90 % NH<sub>3</sub> [25], 93 % [10] and 98.5 % [16] NH<sub>3</sub>.

NH<sub>3</sub>-containing mixtures generate nitrous oxide (N<sub>2</sub>O) whose global warming potential is about 300 times higher than that of CO<sub>2</sub>. A number of studies presented in Table 1 report N<sub>2</sub>O emissions [5–7,16–20,24,25,29]. The parameters whose influence on N<sub>2</sub>O formation have been analyzed are equivalence ratio ( $\phi$ ) [5,7,29]; compression ratio [5,7]; amount of NH<sub>3</sub> or diesel [16–18,24,25]; timing of the main

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[17,19,20,25], pilot [17,18,20,25] and post-injection [17] for CI engines, or spark timing [7] for the SI engine; and the ratio between pilot and main diesel [20,24,25].

The studies summarized in Table 1 span a broad range of conditions and can therefore be expected to result in different levels of pollutant formation, identifying common trends. It was observed that N<sub>2</sub>O emission has a negative correlation with  $\phi$  [5,7], even though Liu et al. [29] reported little variation. In addition to that, in all studies where the main ignition timing was varied [17,19,20,25], delaying the injection lead to an increase of N<sub>2</sub>O. For other quantities, there is a considerable amount of disagreement between studies.

Niki et al. [17] and Jin et al. [25] observed a positive correlation between NH<sub>3</sub> energy fraction and N<sub>2</sub>O, while Førbj et al. [16] reported the opposite. However, in all three studies, there was a positive correlation between N<sub>2</sub>O and unburned NH<sub>3</sub>, and a negative correlation between N<sub>2</sub>O and engine thermal efficiency. Niki [18] advanced diesel injection to 45° and 60° BTDC and observed opposite trends in N<sub>2</sub>O formation with increasing  $X_{NH_3}^E$  for these two regimes. Moreover, in both cases the unburned NH<sub>3</sub> and thermal efficiency increased with  $X_{NH_3}^E$ , contrary to [16,17,25].

Further discrepancies are seen in relation to the time of pilot injection ( $t_{pre}$ ) and diesel split ratio (DSR). Niki et al. [17] and Jin et al. [25] observed negative correlation between  $t_{pre}$  and N<sub>2</sub>O, while Yousefi et al. [20] and Niki [18] had the opposite. All of the above studies had positive correlation between N<sub>2</sub>O and unburned NH<sub>3</sub>, except for Niki et al. [17], who recorded the contrary. Opposite trends between the studies [18,20,25] exist in terms of engine thermal efficiency and N<sub>2</sub>O (or unburned NH<sub>3</sub>) as well. Similarly, disagreement exists in the effect of DSR on N<sub>2</sub>O [20,24,25].

Among the reviewed studies, two distinct explanations to the formation of N<sub>2</sub>O are presented. Westlye et al. [7] proposed that N<sub>2</sub>O is formed during expansion and exhaust strokes. Unburned NH<sub>3</sub> released from crevice volume is mixed with product NO<sub>x</sub>, and N<sub>2</sub>O is formed via the selective non-catalytic reduction mechanism (SNCR, or DeNO<sub>x</sub>). This mechanism was subsequently referred to by Mounaïm-Rousselle et al. [5] and Førbj et al. [16]. The second mechanism, advocated by Jin et al. [25] and Mi et al. [24], assumes that N<sub>2</sub>O is produced at the flame front and is not immediately consumed due to incomplete (disrupted)

combustion. Niki et al. [17] lists both mechanisms as possible pathways for N<sub>2</sub>O formation. Several authors discuss correlation between temperature and N<sub>2</sub>O, however, both of the described mechanisms, in this work referred to as the “DeNO<sub>x</sub>” and “disrupted flame” mechanisms, respectively, require low temperature for N<sub>2</sub>O to be either produced (DeNO<sub>x</sub>) or sustained (disrupted flame): SNCR window is ca. 1100–1400 K [2], while any N<sub>2</sub>O produced at the flame front would decompose via.



if temperature stays sufficiently high (at 1400 K, N<sub>2</sub>O would decrease by an order of magnitude within ca. 20 ms, and within ca. 2 ms at 1600 K). Therefore, unless N<sub>2</sub>O measurements are performed in-situ, neither of the mechanisms can be disqualified, however, all studies in Table 1 report N<sub>2</sub>O from the exhaust.

The disagreement in N<sub>2</sub>O formation trends described above suggests that it is sensitive to a variety of operational parameters, and is a complex product of the effects of flow and chemistry. To increase the understanding of N<sub>2</sub>O formation, and as a result improve mitigation strategies, the effects can be investigated using computational fluid dynamics (CFD) simulations with explicit chemistry schemes. However, due to limitations in computational capacity the reaction schemes need to be compact, but still accurate in the relevant range of conditions. Diesel fuel, frequently seen as the secondary fuel in experimental studies, is often represented by a surrogate such as n-heptane (C<sub>7</sub>H<sub>16</sub>) in the modeling. Concerning NH<sub>3</sub>/n-heptane, there exist several reaction schemes developed for use in CFD, e.g. [30–32]. The two more recent and smaller ones [31,32] contain 67 species and 387 reactions, and 72 species and 495 reactions, respectively (Ar and He not counted, reversible reactions count as 1). These mechanisms are on the upper limit of what can be used in the relevant CFD models. The broad engine operating conditions reviewed above, and the DeNO<sub>x</sub> mechanism for N<sub>2</sub>O formation were not targeted in development of the existing reduced mechanisms for NH<sub>3</sub>/n-heptane.

In the present work, a new reduced scheme is presented, developed for engine-relevant conditions, covering various operational strategies. It also accounts for different pathways for N<sub>2</sub>O formation. Combustion and oxidation of NH<sub>3</sub>/n-heptane was analyzed using 0D and 1D ideal

**Table 1**  
Overview of experimental studies with NH<sub>3</sub> and different secondary fuels, in IC engines.

Source	Year	Ignition type	Second fuel	NH <sub>3</sub> , % energy	NH <sub>3</sub> injection method	Engine speed, RPM (min <sup>-1</sup> )	P <sub>max</sub> , atm	N <sub>2</sub> O meas.
Mounaïm-Rousselle et al. [5]	2021	SA-CI	neat NH <sub>3</sub>	100	Premixed	650–2000	40–80	yes
Liu et al. [6]	2023	SI, TJI	neat NH <sub>3</sub>	100	Premixed	800	25–40	yes
Westlye et al. [7]	2013	SI	H <sub>2</sub>	0–84	Premixed	1000	15–45	yes
Lhuillier et al. [8]	2021	SI	H <sub>2</sub>	0–66	Premixed	1500	40–55	no
Pandey et al. [9]	2023	SI	H <sub>2</sub>	0–76	Premixed	1800	40–50	no
Pyrc et al. [10]	2023	SI	H <sub>2</sub>	30–93	Premixed	600	30–38	no
Oh et al. [12]	2021	SI	natural gas	0–28	Premixed	840	21–27	no
Oh et al. [13]	2022	SI	natural gas	0–20	Premixed	1100	<62	no
Wei et al. [11]	2023	SI	natural gas	0–37	Premixed	1190	45–60	no
Gross and Kong [14]	2013	CI	DME	0–30	Direct	2200–2550	60–75	no
Ryu et al. [15]	2014	CI	DME	0–49	Direct	1900–2500	50–80	no
Førbj et al. [16]	2023	CI	n-heptane	80–98	Premixed	1200	~50	yes
Niki et al. [17]	2019	CI	diesel	0–15	Premixed	1362	60–70	yes
Niki [18]	2021	CI	diesel	45	Premixed	1500	80–110	yes
Yousefi et al. [19]	2022	CI	diesel	0–40	Premixed	910	80–90	yes
Yousefi et al. [20]	2022	CI	diesel	0–40	Premixed	910	80–100	yes
Zhang et al. [21]	2023	CI	diesel	0–50	Direct	375	~60	no
Sun et al. [22]	2023	CI	diesel	0–80	Premixed	1000	22–38	no
Wu et al. [23]	2023	CI	diesel	N/A	Premixed	1500	70–75	no
Mi et al. [24]	2023	CI	diesel	40–70	Premixed	1500	80–110	yes
Jin et al. [25]	2023	CI	diesel	0–90	Premixed	1000	70–100	yes
Elumalai and Ravi [26]	2022	CI	biodiesel	0–50	Premixed	1500	40–83	no
Ryu et al. [27]	2014	SI	gasoline	0–78	Direct	1800	15–16	no
Liu et al. [28]	2023	SA-CI	gasoline	0–28	Premixed	1500–2000	60–70	no
Liu et al. [29]	2023	SI-TJI	H <sub>2</sub> , CH <sub>4</sub> , gasoline	N/A	Premixed	800	20–40	yes

SI – spark ignition; CI – compression ignition; SA-CI – spark-assisted CI; TJI – turbulent jet ignition; N<sub>2</sub>O meas. – N<sub>2</sub>O measurements reported in source.

reactor models, and the target space for reduction (including pollutants) was thoroughly constructed. During reduction, these 0D and 1D reactors were utilized simultaneously. The performance of the mechanism in engine-relevant conditions is discussed and compared to literature models [31,32].

## 2. Methods

In this work, the Ant-Colony Reduction (ACR) method developed by Pichler [33] is utilized, in combination with manual steps. The combined methodology is motivated by the challenge to construct a compact dual-fuel mechanism for two fuels with such varying reactivity, and over wide range of conditions.

ACR is a semi-stochastic build-up mechanism generating algorithm with a customizable target function that accommodates multiple reactor models, scalar and vector target quantities, and it generates mechanisms with a very low number of reactions. During reduction, performance in the whole target space acts as feedback to the mechanism-generating algorithm. This marks a difference to a more common approach where mechanisms are tested against a broader target space at the validation stage. The use of multiple reactor geometries during reduction is an advantage compared to, e.g., commercially available reduction package in CHEMKIN [34].

As initial steps before a mechanism reduction, a detailed target mechanism and appropriate reactor models capturing the relevant combustion targets need to be selected. Also, the reduction space must be defined in terms of initial parameters, such as  $\text{NH}_3$ /n-heptane mixture composition, stoichiometry, temperature, pressure and characteristic time scales. The selected entities must be adequate and relevant to the engine conditions, moreover, the end result is greatly affected by these initial choices, therefore, the selection process is described in detail below.

### 2.1. Selection of the reactor models

As discussed in Section 1, in IC engines,  $\text{NH}_3$  can be either premixed with air at intake or injected directly. Also, diesel fuel might contain a pre- or post-injected component. To accommodate for such different injection strategies, it was decided to target both ignition and flame propagation during reduction stage, by using the closed homogeneous 0D reactor and 1D free-propagating flame, respectively. The corresponding target quantities are ignition delay time (IDT) and laminar burning velocity (LBV).

Additional targets were selected in order to account for the two possible mechanisms of  $\text{N}_2\text{O}$  formation proposed in the experimental studies, i.e., the disrupted flame mechanism and the  $\text{DeNO}_x$  mechanism. First, the “1D flame” component of the ACR target function was extended with  $\text{N}_2\text{O}$  and NO concentrations. A correct prediction of NO formation is necessary, as NO is a reactant in the  $\text{DeNO}_x$  mechanism. This process was in turn represented by modeling oxidation of  $\text{NH}_3/\text{O}_2/\text{N}_2$  mixtures in presence of NO at high pressures and intermediate temperatures in adiabatic 0D reactors, and  $\text{N}_2\text{O}$  temporal profiles were targeted.

### 2.2. Selection of the initial mixture parameters

Table 2 contains information on the selected range of initial mixture parameters for each of the three types of reactors used during the reduction process. Range of pressure was determined directly from the literature analysis presented in Table 1. The upper border of the characteristic timescale of  $\sim 10^{-1}$  s, which served as the maximal allowed IDT and the oxidation end time, corresponds to  $60^\circ$  CAD piston movement in a slowly operating marine engine  $\sim 100$  RPM. The lower temperature limit of 600 K for ignition cases corresponds to a pressure of ca. 10 atm at the end of compression, and at the same time, to 0.1 s IDT of pure n-heptane at 100 atm (i.e., no ignition faster than 0.1 s is possible

**Table 2**

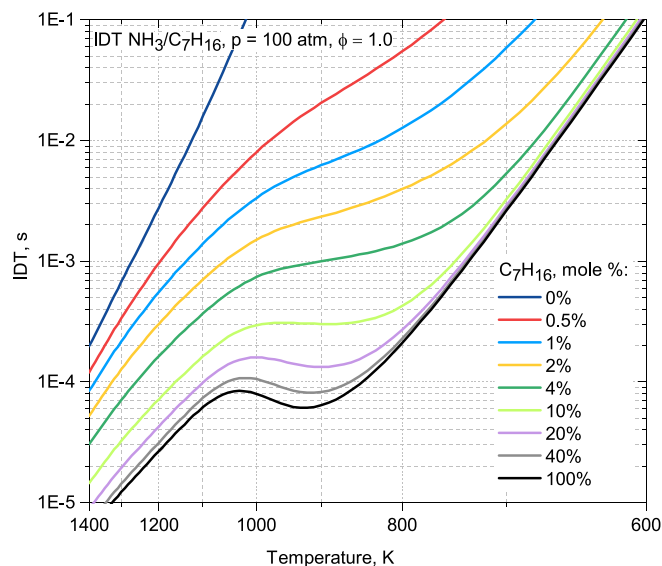
Mixture parameters for each of the implemented reactor models.

reactor type	0D $C_v$	1D flame	0D $C_p$
target	IDT	LBV, $\text{N}_2\text{O}$ , NO	$\text{N}_2\text{O}(t)$
time scale, s	$\leq 0.1$	N/A	$\leq 0.1$
$p$ , atm	10–100	10–100	10–100
$T_0$ , K	600–1400	500	800–1400
$\phi$	0.5–1.5	0.7–1.3	0.6–1
$X_{\text{NH}_3}$ (mol. %)	0–100 %	0–100 %	100 %
No. cases	553	11	62

$C_v$  and  $C_p$  – constant volume and constant pressure reactors, respectively.

below 600 K). The temperature window for the  $\text{DeNO}_x$  oxidation cases depends on residence time and pressure; therefore, its lower boundary turned out to be somewhat lower than specified in [2] due to higher pressures. For flame simulations, a single elevated temperature of 500 K was selected, a temperature where auto-ignition does not yet occur. One temperature was found to be sufficient since temperature dependence of LBV has a weak dependence on chemistry compared to LBV itself [35].

Despite that in the majority of the experimental engine studies listed in Section 1,  $\text{NH}_3$  is premixed with air at the inlet, the diesel fuel is still injected directly, leading to a variety of local equivalence ratios in the combustion chamber. According to Mastorakos [36], in non-premixed combustion, the stoichiometric mixture fraction is not directly related to the most reactive mixture fraction, and the latter is most often located at the lean side [36]. Therefore, it was decided to vary  $\phi$  to both lean and rich sides for ignition and flame cases, while for the  $\text{DeNO}_x$  oxidation it is assumed that  $\text{NH}_3$ /air ratio cannot exceed stoichiometric (since unburned  $\text{NH}_3$  from crevices had to be premixed at inlet). Several experimental studies [10,16,25] achieved a stable engine operation when the energy fraction of  $\text{NH}_3$  in the fuel was kept near or above 90 %. When recalculated to mole fractions, more common in kinetic studies, and assuming the second fuel to be n-heptane, it equals 99 %. The two fuel components,  $\text{NH}_3$  and n-heptane, have a qualitatively different ignition behavior. Fig. 1 presents IDT of  $\text{NH}_3$ /n-heptane, calculated with the detailed mechanism by Thorsen et al. [37] and constrained by the upper time limit of 0.1 s, for the complete range of n-heptane mole fractions. As little as 0.5 % n-heptane by mole (7 % by energy) significantly accelerates ignition and affects its temperature dependence, while after about 40 %, the IDT closely resembles pure n-heptane. To preserve such behavior in the reduced mechanism, the reduction target space contained mixtures ranging from 0 % to 100 % n-heptane (specifically, 0,



**Fig. 1.** IDT of stoichiometric  $\text{NH}_3$ /n-heptane mixtures at 100 atm with varied fraction of n-heptane calculated with the mechanism of Thorsen et al. [37].

0.5, 2, 10, 40 and 100 % by mole).

The influence of the mixture composition on the LBV of NH<sub>3</sub>/n-heptane, when expressed in mole fractions, is also non-linear, as evident from the work of Lubrano Lavadera et al. [38]. The dependence becomes quasi-linear if mass fractions are adopted. The kinetic analysis in that work has shown that for LBV no direct chemical coupling effect needs to be considered. As flame simulations are computationally heavy compared to IDT, the target space in the present work is limited to mixtures with 0, 50, and 100 % NH<sub>3</sub> (by mole).

For the DeNO<sub>x</sub> N<sub>2</sub>O formation, only mixtures without carbon-containing species were considered during reduction, since the oxidation is expected to occur when products (containing NO) mix with the NH<sub>3</sub>/air mixture. For the studied conditions, no chemical effects of CO<sub>2</sub> or H<sub>2</sub>O were observed in test runs, and the influence of CO will be discussed separately in Section 3. In present work, it was assumed that reaction



has a much slower rate at low and intermediate temperatures than in [37], leading to a more limited chemical effect of CO than was predicted by [37].

The proportions of initial DeNO<sub>x</sub> reactants: NH<sub>3</sub>, air, the product gas and NO in the real engine simulations are not known a-priori, therefore, for modeling consistency, the amount of the inert component (N<sub>2</sub>) in the O<sub>2</sub>/N<sub>2</sub> oxidizing mixture was varied, and the concentration of NO was assumed to be 0.1 % by mole.

### 2.3. Selection of chemical mechanisms

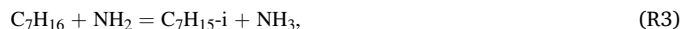
It has been shown that subset of reactions between carbon- and nitrogen-containing species is necessary for representing ignition of binary NH<sub>3</sub>-containing fuels (see, e.g., [39–41]). For NH<sub>3</sub>/n-heptane, dedicated detailed mechanisms that include interaction subsets were developed only recently [37,42]. Therefore, the reduced mechanism by Wang et al. [32] employed the model of Dong et al. [42] as target, but earlier models by Liu et al. [30] and Xu et al. [31] were developed without considering any interaction chemistry.

In the present study, the mechanism of Thorsen et al. [37] was selected as the target mechanism. This model is based on the continuously updated Glarborg mechanism [2,43] and the detailed n-heptane mechanism of Zhang et al. [44]. The C3-C7 interaction subset [37] was developed with the aim to simulate ignition of NH<sub>3</sub>/n-heptane mixtures at 10–15 bar available from [45], and oxidation of these mixtures in jet-stirred and flow reactors at pressures up to 100 bar [37]. The Supplementary Material (SM) contains additional validation for the mechanism [37] against the experiments of [38,42] (Figs. S6,S7). Note that all IDT [42,45] and LBV [38] experimental data for NH<sub>3</sub>/n-heptane mixtures is largely outside the target space considered in the present study due to either pressure [38] or type and amount of dilution [42,45]: only one IDT dataset at the lower pressure border (10 atm) and with a rather narrow temperature window from [42] can be considered (see Fig. S6). Therefore, reliability of the predictions of the target mechanism [37] had to be assumed inside the target space of the present study.

Prior to reduction, an intermediate base model was constructed by merging subsets of reactions for n-heptane, NH<sub>3</sub> and their interactions, following the approach of Wang et al. [32]. The n-heptane sub-mechanism of the reduced model [32], which itself is a modified version of the reduced model of Chang et al. [46], was merged with the detailed H/N/O and the C/H/N/O submechanisms of Thorsen et al. [37], keeping the hydrogen submechanism from [37]. As will be discussed in the results section, the rates of the key reactions in the H/N/O sub-mechanism in the base/target mechanisms are a major contributor to the observed differences in the performance of the reduced mechanisms analyzed in the present work, therefore, we rely on most recent updates in the H/N/O subset by Glarborg [43], that were implemented into the

target mechanism [37].

The C3-C7 interaction subset was based on the target mechanism [37]. Rates of reactions of the same classes as in [37] were reconstructed for the C3-C7 hydrocarbon species present in [32]. For reactions that required lumping, e.g.



where  $i = 1, 2, 3, 4$  denotes one of the four heptyl isomers, forward and reverse channels were entered separately, i.e.:



with the forward rate constant being a 3-term fit of the sum of the corresponding rate constants in the temperature range of 300–2500 K, and the reverse rate being a 3-term fit of a weighted sum of the reverse rate constants for the primary and secondary heptyl radicals, with a branching ratio (weight) calculated approximately using the forward rates. Overall, the merged mechanism contained 143 species and 989 reactions.

Some rate constants were optimized or modified to improve the performance of the base mechanism in terms of LBV and IDT, in comparison to the target mechanism [37]. The process is reported in detail in the SM. To improve LBV, three reactions from the C2-C3 subset were modified, and for ignition, A-factors of 18 reactions were optimized. These 18 reactions were either from the C7 fuel breakdown subset of [32,46], where rates are to some extent artificial by design, or from the C/N interaction subset, where many rates were estimated in the present work. These reactions can thus be considered to have large uncertainty limits. With such approach, the full NH<sub>3</sub> submechanism remained intact from the target model [37]. Optimization was performed with the differential evolution algorithm, similar to previous work [47].

The exact reactions for optimization were selected after performing a global sensitivity analysis as described in the SM. All optimized reactions with their rate constants are listed in the SM. The comparison between the base and the target mechanisms can be viewed in Figs. 2–4, where some selected conditions are presented, while the whole target space is reported in the SM. Typically, some discrepancy was observed between the base and target mechanisms even after optimization in terms of IDT at low temperatures (see Fig. 2), especially in mixtures with lowest amount of n-heptane. For LBV, 100 % n-heptane was reproduced

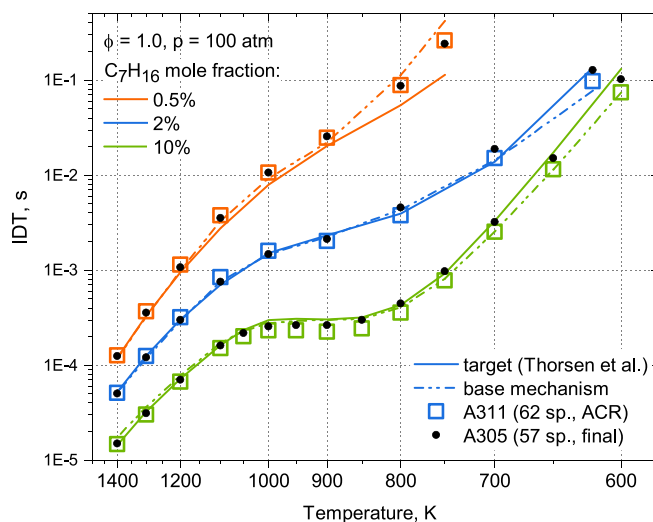


Fig. 2. Ignition delay times for three NH<sub>3</sub>/n-heptane mixtures. Solid lines: target mechanism [37], dashed lines: base mechanism, squares: initial 62-species mechanism after ACR reduction (A311); black dots: final 57-species mechanism (A305).



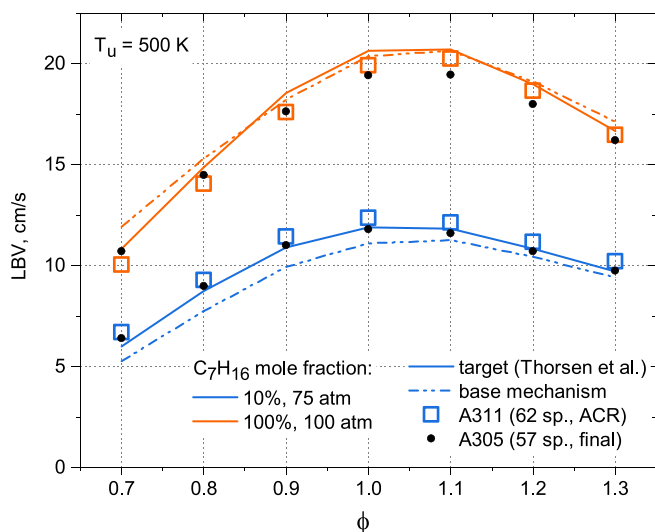


Fig. 3. Laminar burning velocities for  $\text{NH}_3/\text{n-heptane} + \text{air}$ . Lines and symbols correspond to same mechanisms as in Fig. 2.

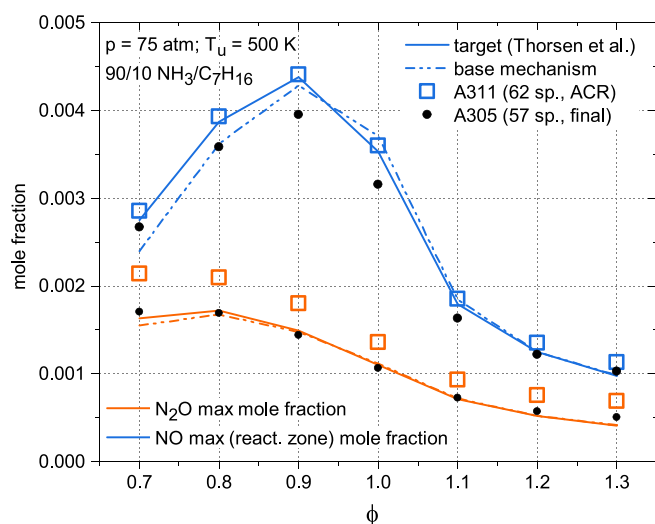


Fig. 4. Maximal (reaction zone) mole fractions of  $\text{N}_2\text{O}$  (orange) and  $\text{NO}$  (blue). Lines and symbols correspond to same mechanisms as in Fig. 2. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

better than binary mixtures (see Fig. 3 and Fig. S9 in SM). Implementation of the lumped and reduced n-heptane submechanism also affected pathways for  $\text{NO}$  formation, as can be seen in Fig. 4 and Figs. S11-S13 in SM. Overall, however, the performance of the base model was satisfactory for subsequent reduction.

#### 2.4. Reduction procedure

The ACR Python code [33] has been used previously to obtain reduced mechanisms for high-pressure n-heptane combustion [48]. In the present work, the ant colony ran in a single target space including IDT, LBV, and species profiles in 0D and 1D reactors. Predictions of the detailed mechanism [37] were used as targets, while the starting point for the reduction was the base merged model described above. Several reactions were marked as “important” and forced to be included into all generated mechanisms. A number of reactions from the  $\text{NO}_x$  subset, which do not belong to major reaction chains, were included manually. The preferred approximate range of sizes of the generated mechanisms

can be selected before reduction, this was done after preliminary runs by finding an optimal trade-off between mechanisms’ size and their accuracy. The final candidate mechanism was selected from the generated mechanism pool based on the overall averaged accuracy, the average accuracies of each target quantity, maximal deviations from target for each target quantity, and on the mechanism size. The work was focused on determining an optimal set of initial settings to maximize the accuracy of the best ant-generated mechanism, without relying heavily on subsequent optimization as in [48]. Only five rate constants were re-optimized after reduction (see Table S2 in the SM).

The ACR code is integrated with Cantera 2.4.0 [49] Python libraries, while both Cantera and Chemkin 2020 R2 [34] were used for validation and analysis. While less strict solver parameters, e.g., the allowed gradient between grid points for the flame simulations (GRAD) were used during reduction, for figures in this article, the GRAD parameter was set to 0.025 (0.06 for [37] due to its size), resulting in at least 300 grid points. In 0D simulations, the absolute and relative solver tolerances were set to at least  $1\text{E-}20$  and  $1\text{E-}9$ , respectively. Ignition was determined at the inflection of the temperature profile. In flames, mixture-averaged formulation of the transport properties was set.

After ACR reduction, a candidate mechanism (A311) with 62 species and 161 reactions was selected. Its performance characteristics are presented in Table 3. Please note that in this table and throughout the paper, accuracy is defined as a sum of absolute mean changes for each target case:

$$A = \frac{1}{n} \sum_{i=1}^n \frac{|y_i - y_i^0|}{\max(y_i, y_i^0)} \times 100\%$$

where  $y_i$  and  $y_i^0$  are evaluated quantities for the reduced and target models, respectively, and  $n$  is a number of targets of the same kind (e.g., IDT or LBV). In case of the overall accuracy, accuracies are weighted over each of the target quantities presented in Table 3. Table S3 in the SM lists all 626 modeling cases that correspond to the target space of Tables 2 and 3 with the corresponding weight functions for each of the target quantity.

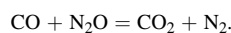
The mechanism A311 was further modified and reduced manually, and a few rate constants were optimized, with a goal of achieving smaller size while preserving (or even improving) the overall accuracy. As ACR is a semi-stochastic build-up method, certain reactions important to a smaller subset of targets might be omitted by the algorithm. In addition to that, it is possible to manually remove species while keeping the corresponding reaction pathways by reaction lumping. These manual steps were performed by validating the test versions of the mechanism against the same target space as during the ACR reduction. All manual steps are listed in Table S4 in the SM and are outlined below.

First, to improve performance in terms of  $\text{N}_2\text{O}$  profiles in flames, three reversible reactions were added, which were initially omitted by ACR. Next, few species were further removed, either with all their reactions, or reaction chains were bundled together, eliminating intermediate steps. To ensure compatibility with CFD solvers such as OpenFOAM [50], reactions with pressure dependence through logarithmic interpolation (PLOG) were expressed as pressure-independent. Two PLOG reactions remained in the mechanism after reduction, and only one of them possessed pressure dependence in the 10–100 atm applicability range of the mechanism, that is reaction



For (R5), rate coefficient at 10 atm was simply taken, as its pressure dependence in the 10–100 atm pressure range was found to be weak.

It was decided to replace rate coefficients of reaction (R2), i.e.



added at the first step, to an expression determined by Loirat et al. [51]. This value is implemented in, e.g., the Konnov detailed mechanism [52].

**Table 3**  
Size and performance of the target, intermediate and final mechanisms.

mech.	species	reactions			accuracy, %					
		total	rev.	irrev.	overall	N <sub>2</sub> O <sup>fl</sup>	NO <sup>fl</sup>	LBV	IDT	N <sub>2</sub> O <sup>fr</sup>
target	1367	6314	5228	1086	100	100	100	100	100	100
base	143	989	942	47	92	98	91	98	90	100
A311	62	161	150	11	87	87	91	94	86	86
A305	57	158	145	13	89	95	88	96	89	87

Target: target mechanism [37], base: base mechanism; A311 – after ACR reduction, A305 – final version; (ir)rev. – (ir)reversible; fl – flame; fr – flow reactor (DeNO<sub>x</sub> mechanism).

In the target mechanism [37], expression recommended in the review of Tsang and Herron [53] is used. The two rates are similar at high temperatures, however, the difference at  $\sim 700$  K becomes around  $10^5$ , resulting in qualitatively different N<sub>2</sub>O predictions for NH<sub>3</sub>/NO oxidation cases in presence of CO and before ignition of NH<sub>3</sub>/n-heptane mixtures, as shown in Section 3.3 and SM. Since [53], there appeared several studies questioning the preferred rate constant [53]. Wang et al. [54] calculated the activation barriers for a number of direct and indirect transitions, and their values were in agreement with the activation energy of 46 kcal/mol of Loirat et al. [51]. Recently, Krupnov and Pogosbekian [55] calculated potential energies and rate constants for this reaction, and they appeared to be in qualitative agreement with [51], but  $\sim 200$  to 10 times slower at  $T = 600$ – $2000$  K, respectively (see Fig. S3 in SM). Considering that [51] and [53] agree at  $T \approx 2000$  K, in the present work, an expression from [51] was adopted.

Next, reactions from the previously optimized subset were once again revisited. Five reactions received new rate constants following re-optimization. During the process, the A-factors were allowed to change only in direction that would bring them closer to the corresponding values in the detailed mechanism [37]. Finally, two reactions:



were inserted following additional analyses that will be described in Sections 3.2.2 and Sections 3.3, respectively. Table S4 in the SM lists all manual changes providing details on the rate constants. The final version of the mechanism is presented in Table 3 as A305. It is provided in Chemkin and Cantera formats in the SM.

The applicability range of the mechanism is determined by the target space parameters of Table 2, e.g., pressure range 10–100 atm, NH<sub>3</sub> fractions 0–100 %, NO and N<sub>2</sub>O formation etc. One exception that is outside the target space of the present work is NO formation in rich 100 % n-heptane mixtures (see Fig. S13), which are of little practical relevance. The reduced mechanism of the present work is supposed to be used only under conditions listed in Table 2.

Figs. 2-4 illustrate the performance of intermediate versions of the mechanism and its final version at selected conditions, while the whole target space can be found in the SM. Since reduction was performed targeting the detailed mechanism [37], the reduced models were found to be closer to the target mechanism than to the base mechanism at certain conditions. All mechanisms perform qualitatively similar, and quantitative difference was measured by accuracy scores as reported in Table 3. In particular, predictions of N<sub>2</sub>O in flames of NH<sub>3</sub>/n-heptane mixtures by the A305 mechanism have significantly improved compared to A311 due to addition of reactions, e.g. (R2), as well as



Reaction (R8) competes with high-temperature formation route of N<sub>2</sub>O [2]:



Due to (R8), accuracy of NO predictions has slightly lowered (see Fig. 4), however, since N<sub>2</sub>O accuracy has increased to a larger degree,

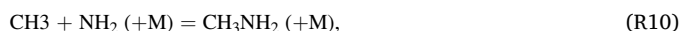
(R8) was kept in the final mechanism.

### 3. Results

#### 3.1. Composition of the mechanism

The reduced mechanism developed in the present work and literature models [30–32] are intended to be used in CFD, however, they are produced with different methodologies and have different number of species and reactions in their constituent submechanisms, as seen in Table 4. The A305 mechanism is significantly smaller compared to the others, in terms of both reactions and species, while maintaining an overall good accuracy. To understand the differences in performance between the mechanisms, analysis of composition of different reaction subsets is necessary. In the later comparison of modeling results also the difference in size should be considered as a factor when judging the overall performance and usefulness of the A305 mechanism.

The hydrocarbon submechanisms of A305, Xu et al. [31] and Wang et al. [32] are all based on a multi-fuel model of Chang et al. [46], whose size for n-heptane is also listed in Table 4. The model of Xu et al. [31] contains 10 more species than A305, and this difference comes from 5 extra nitrogen species and 5 hydrocarbon species. The model of Xu et al. [31] has the largest NH<sub>3</sub> submechanism, as it is in fact a detailed H/N/O mechanism [56] with one modified reaction. In turn, the size of the NH<sub>3</sub> submechanism of Wang et al. [32] is comparable to A305 (in terms of species). The main difference between A305 and [32] comes from the C/H/N/O submechanism. The model [32] was developed to predict, among other things, emissions of HCN, and preserving the cyanide submechanism came at a cost of 10 extra species and 121 extra reactions. In the present work, it was observed that in addition to emission formation, the cyanide pathway that starts with formation of methylamine



**Table 4**  
Composition of the NH<sub>3</sub>/n-heptane reduced models.

mech.	species <sup>1</sup>					reactions <sup>1,2</sup>		
	total	H/ O	N/ H/ O	C/H/ O	C/ H/ N/O	total	H/O + C/H/O	C/H/ N/O
Thorsen <sup>3</sup> [37]	1365	9 <sup>4</sup>	23	1257	75	6310	5322	792
A305	57	8	16	33	0	159	96	9
Xu [31]	67	8	21	38	0	387	207	0
Wang [32]	72	8	17	37	10	495	185	156
Liu [30]	103	8	20	75	0	572	392	0
Chang <sup>5</sup> [46]	47	8	N <sub>2</sub>	38	N./ A.	207	207	N./ A.

<sup>1</sup> species Ar and He (present in some models) and their reactions are not counted.

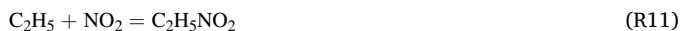
<sup>2</sup> reversible reactions count as 1.

<sup>3</sup> detailed target mechanism for A305.

<sup>4</sup> O<sub>3</sub> not counted (no reactions).

<sup>5</sup> n-heptane mechanism.

plays a role in modeling IDT with reduced mechanisms, as well as nitroethane pathway via



Larger mechanisms generated by the ACR method did contain the corresponding pathways. In smaller mechanisms, including the selected candidate, the (inhibiting) effect of these pathways is compensated by absence of some other (accelerating) pathways.

Despite that A305 does not contain any C/N species, interaction reactions between C and N species play a major role through H- and O-atom exchange reactions. The most important is H-abstraction from n-heptane by  $\text{NH}_2$  (R4). The A305 mechanism also contains four other H-abstraction reactions by  $\text{NH}_2$ , two reactions of  $\text{NO}_2$  and reactions (R2, R7) of CO and  $\text{N}_2\text{O}/\text{NO}_2$  discussed in Section 3.3. This sums up to 9 reactions in the C/H/N/O subset, compared to 156 in Wang et al. [32], of which 35 are unrelated to the cyanide subset.

### 3.2. Performance of the mechanism

#### 3.2.1. Ignition

Fig. 5 presents IDT of mixtures of  $\text{NH}_3$  and n-heptane with varied percentage of n-heptane in the panels: 0 %, 0.5 %, 2 %, 10 %, 40 % and 100 % by mole. In this figure, pressure and  $\phi$  are fixed at 100 atm and 1.0, respectively, as it is sufficient to illustrate all observed trends. Data for the complete target space (see Table 2) are reported in the SM (Figs. S8-S14). The current mechanism is compared to its target [37] and the reduced mechanisms of Xu et al. [31] and Wang et al. [32]. The mechanism of Liu et al. [30] was not considered due to its large size compared to other models (see Table 4). The Dong et al. model [42] served as target in development of [32] and is therefore included in figures for fair comparison of [32], whereas the mechanism of Xu et al. [31] did not have a target mechanism. It should be noted here that the A305 is considerably more compact than the other two mechanisms (see Table 4).

The present mechanism closely follows its target [37], except for the low-temperature region for mixtures with lowest n-heptane content: 0 % and 0.5 % (Fig. 5a,b). The performance of the Wang et al. [32] mechanism compared to its target [42] is better for neat  $\text{NH}_3$  and similarly mediocre for the 0.5 % mixture, but in the 2 % mixture it has large deviations from both detailed models. The mechanism of Xu et al. [31] is qualitatively different to the rest, as it predicts no NTC in the 0.5 % and the 2 % n-heptane cases. In addition to that, it deviates from the other models for the 10 % n-heptane mixture in the low-temperature region. These trends are similar for mixtures at other equivalence ratios and slightly different at lower pressures, see Fig. S8 in the SM.

Overall, the present mechanism and Wang et al. [32] can be viewed comparable in terms of ignition performance, while Xu et al. [31] fails to reproduce all conditions in the selected space, most probably [37], due to absence of C-N interactions, which the two other reduced mechanism do contain. As for the Wang et al. model [32], its overall accuracy against the target [42] (calculated in the same space) is equal to 83 % suggesting that mixtures with very low n-heptane content were outside the target space of Wang et al. [32].

This, again, illustrates the fact that reduced mechanisms should not be used outside of their target spaces. Diesel fuel has a much higher energy density than  $\text{NH}_3$ . Even for n-heptane, a small amount of it enhances ignition properties of  $\text{NH}_3$  by an order of magnitude, therefore to correctly capture ignition in non-uniformly mixed environments, low-percentage n-heptane mixtures have to be taken into account.

#### 3.2.2. Laminar flames

For the 1D free-propagating flames, the reduction space included LBV and NO and  $\text{N}_2\text{O}$  profiles in mixtures of  $\text{NH}_3$  + air, n-heptane + air, and 50/50  $\text{NH}_3$ /n-heptane + air. For validation, mixtures with other compositions were analyzed as well, and the results can be found in the

SM (Fig. S9).

Fig. 6a shows LBV of  $\text{NH}_3$ /air mixtures at  $T = 500$  K and pressures of 10 and 100 atm. While good performance of all versions of the present mechanism was observed at 100 atm, the 10 atm, 100 %  $\text{NH}_3$  case is where deviations between its intermediate version and the target were maximal (see Fig. S9(a,c) in the SM). A sensitivity analysis for LBV has shown that insertion of the terminating channel (R6) resolves the disagreement, so A305 closely follows the target at both pressures (Fig. 6a). The influence of this high-temperature biradical reaction (R6) is limited to flames at lower pressures and with high  $\text{NH}_3$  content. All other flames analyzed in this study are unaffected by (R6).

For  $\text{NH}_3$ -air flames of Fig. 6a, the mechanism of Wang et al. [32] closely follows its target [42]. The situation is different when n-heptane is either a sole fuel or is in 50/50 proportion with  $\text{NH}_3$  (Fig. 6b). There the present mechanism is closer to target, than Wang et al. [32], especially in rich mixtures. However, the differences between the two reduced mechanisms and their respective targets are on the same level or less than the difference in prediction between the two detailed mechanisms of Thorsen et al. [37] and Dong et al. [42], disallowing direct comparison of the two reduced mechanisms. Same (as for [32]) can be said about the mechanism of Xu et al. [31]. As discussed above, for LBV, direct interactions between hydrocarbon and nitrogen-containing species are of low importance. Only a few reactions of NO,  $\text{NH}_2$  or  $\text{NO}_2$  with hydrocarbon species have appeared in the LBV sensitivity analysis performed for Thorsen et al. [37] mechanism and conditions of Fig. 6b, but their importance can be concluded to be negligible.

Fig. 7 presents maximal mole fractions of  $\text{N}_2\text{O}$  and NO for two  $\text{NH}_3$ /n-heptane mixtures with 50/50 (top) and 90/10 (bottom) composition at  $T = 500$  K and  $p = 75$  atm, while all other validation conditions can be found in the SM. While for the case of  $\text{N}_2\text{O}$  the maximal mole fractions are always located at the flame front, for  $\phi \leq 0.9$  in the 50/50 mixture (Fig. 7c) and  $\phi \leq 0.8$  in the 90/10 mixture (Fig. 7d), NO formation continues in the post-flame zone, for these conditions, maximal values at the flame front are plotted.

Here, the present mechanism predicts  $\text{N}_2\text{O}$  very close to the target, while for NO there are small deviations near stoichiometric mixtures. However, post-flame NO is reproduced correctly (see NO values at 1 cm above the flame in Fig. 7). The mechanism of Wang et al. [32] reproduces maximal NO concentrations perfectly, while predictions of  $\text{N}_2\text{O}$  in the 50/50 mixture (Fig. 7a) are less satisfactory. The mechanism of Xu et al. [31] is not able to predict  $\text{N}_2\text{O}$ , with the largest discrepancies to both detailed models in lean mixtures. It has to be again noted that prediction of NO in rich flames of pure n-heptane is outside the validation range of the present mechanism, and none of the tested reduced mechanisms were able to reproduce NO there (see Fig. S13 in SM).

#### 3.2.3. Laminar flow reactors

Formation of  $\text{N}_2\text{O}$  in IC engines via the DeNO<sub>x</sub> mechanism was represented by oxidation of  $\text{NH}_3$  in presence of NO in homogeneous constant-pressure reactors, a common configuration in kinetic studies utilized to simulate flow reactor experiments. The main difference of the simulations presented below to real flow reactors is the level of dilution. As the goal of the present study is to reproduce conditions most relevant to IC engines, it is reasonable to investigate undiluted  $\text{NH}_3$ /NO/air mixtures. At the same time, the proportions in which the unreacted  $\text{NH}_3$ /air mixture is mixed with the hot product gas (source of NO) are unknown, for that reason, in the simulations, amount of  $\text{N}_2$  in the  $\text{O}_2/\text{N}_2$  oxidizer mixture varied in a series: 79 %, 89.5 %, 95 %, 99 %. The first percentage corresponds to a hypothetical region with only a trace amount of product gas, the second - to a case where  $\text{NH}_3$ /air mixture and product gas are mixed in approximately equal proportions. The 1/99  $\text{O}_2/\text{N}_2$  resembles a "real" flow reactor case. Due to lower dilution levels, and therefore, a non-negligible heat release, an adiabatic condition was used rather than an isothermal one. A single end time of 0.1 s was selected, as discussed in Section 2. This parameter was varied in the

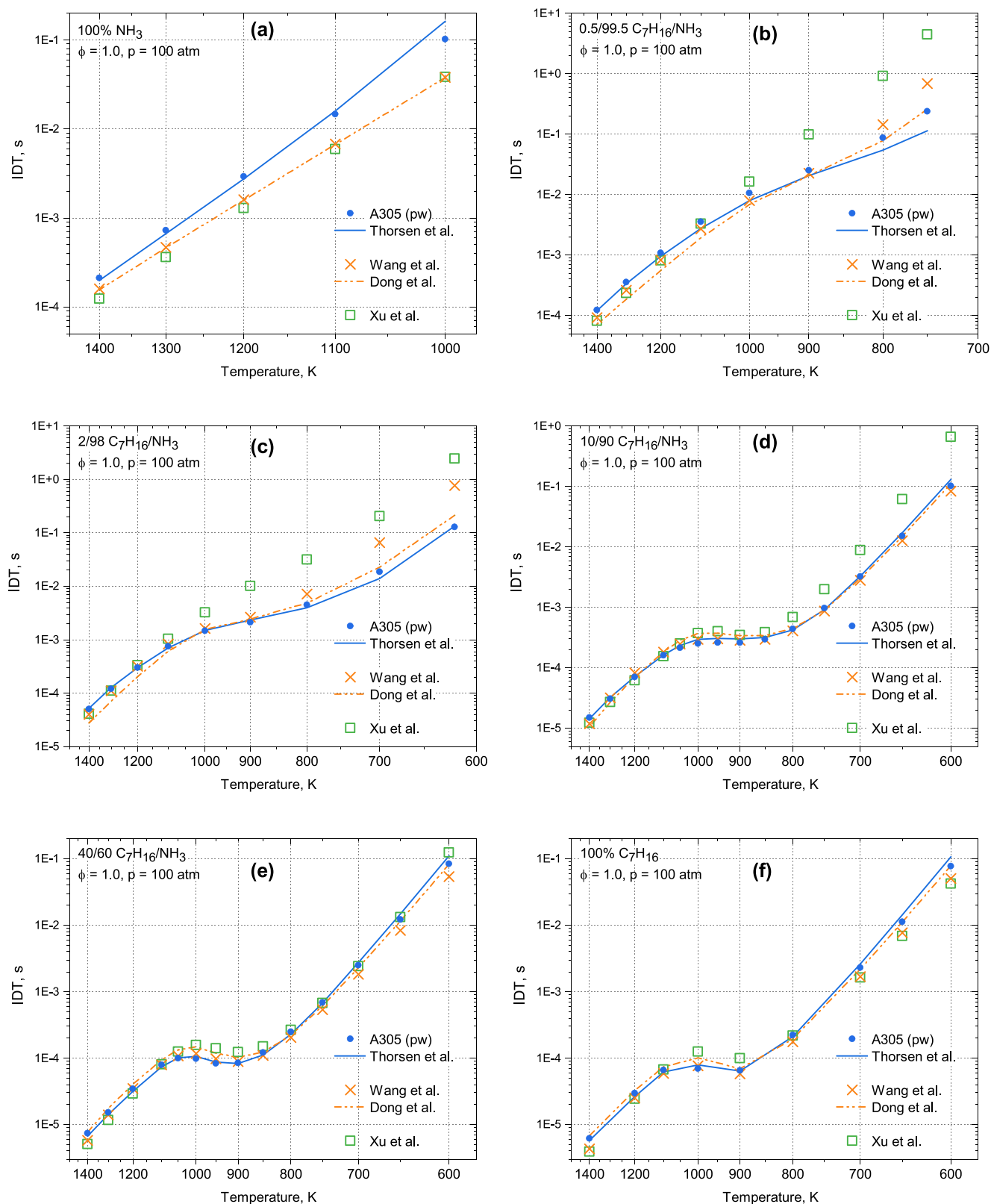


Fig. 5. IDT of  $\text{NH}_3/\text{n-heptane}$  mixtures of variable  $\text{NH}_3$  molar percentage: 100 % (a), 99.5 % (b), 98 % (c), 90 % (d), 60 % (e) and 0 % (f) at 100 atm and  $\phi = 1.0$ ; calculated with the present mechanism (blue dots) and its target [37] (solid lines); Wang et al. [32] (crosses) and its target [42] (dash-dot lines), and Xu et al. [31] (squares). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



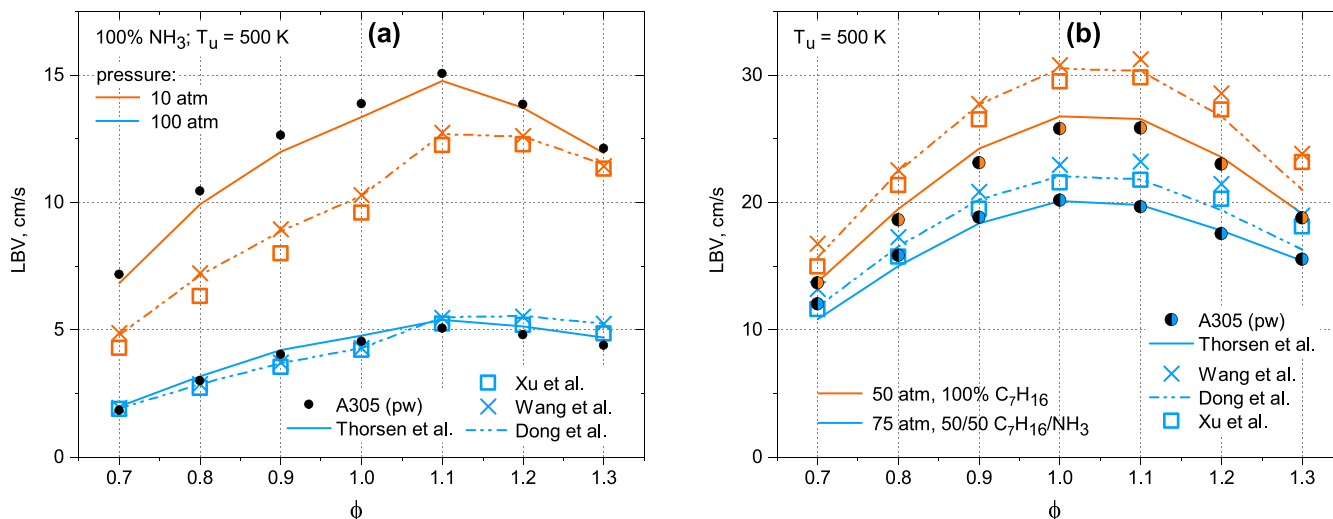


Fig. 6. LBV of NH<sub>3</sub>/n-heptane at different pressures: 100 % NH<sub>3</sub> at 10 and 100 atm (a); 100 % n-heptane at 50 atm and 50/50 mixture (by mole) at 75 atm (b); calculated with the present mechanism (black dots) and its target [37] (solid lines); Wang et al. [32] (crosses) and its target [42] (dash-dot lines), and Xu et al. [31] (squares).

preliminary analysis, and it was concluded that with the selected time, all trends are captured. In this section, the results are presented as N<sub>2</sub>O mole fractions at the end time of 0.1 s, plotted as a function of initial reactor temperature.

Fig. 8 shows selected plots of N<sub>2</sub>O mole fraction at 0.1 s as function of initial temperature for two mixtures: with 10.5/90.5 O<sub>2</sub>/N<sub>2</sub> ratio and  $\phi = 0.6$  (top); and 1/99 O<sub>2</sub>/N<sub>2</sub> with  $\phi = 1.0$  (bottom), while other results are reported in SM (Fig. S14). The effect of pressure is illustrated by left (10 atm) and right columns (100 atm). With rising pressure, N<sub>2</sub>O formation increases, and the DeNO<sub>x</sub> temperature window shifts to lower temperatures. An exactly opposite trend is observed when increasing dilution. Rapid drop of N<sub>2</sub>O at higher temperatures corresponds to auto-ignition occurring at 0.1 s. To illustrate how much initial presence of NO affects formation of N<sub>2</sub>O, Fig. 8a shows a case calculated for the same mixture in which NO is replaced by N<sub>2</sub>. The difference is of about orders of magnitude at lower temperatures, while closer to 0.1 s ignition temperatures, more of NO<sub>2</sub>, necessary for N<sub>2</sub>O production via low-temperature pathway [2].



is formed from NH<sub>3</sub> rather than from NO.

The two reduced mechanisms, of the present work and Wang et al. [32], represent their respective target mechanisms well, except for a case of 10/90 O<sub>2</sub>/N<sub>2</sub> at 100 atm, where the present mechanism deviates by about 25 K in predicting the sharp rise in N<sub>2</sub>O formation. The mechanisms of Xu et al. [31] and the parent of its NH<sub>3</sub> submechanism, the detailed mechanism of Bertolino et al. [56], differ in only one reaction in the NH<sub>3</sub> submechanism (and H<sub>2</sub> submodel in [31] is from [46]), therefore, their predictions are almost identical to each other. However, compared to the rest, they show highest amounts of N<sub>2</sub>O at most conditions.

For these NH<sub>3</sub>/O<sub>2</sub>/NO oxidation cases, major differences are observed between the detailed models: Thorsen et al. [37], Dong et al. [42] and Bertolino et al. [56]. This is best seen in Fig. 8a, where at ca. 1125 K Dong et al. predicts twice as much N<sub>2</sub>O as Thorsen et al., and Bertolino et al. predicts twice as much N<sub>2</sub>O as Dong et al. Reaction analysis has revealed that all difference at this temperature is due to selection of the two rate constants of the key channels



of which the latter is chain-propagating and the former is chain-terminating [57]. Thorsen et al. [37] rely on recent calculations of Klippenstein and Glarborg [57], who predict the termination channel to be about 3–3.5 times faster than propagating in the temperature window of Fig. 8. Dong et al. [42] consider calculations of Stagni et al. [58] for the reverse reaction of (R13), i.e.:



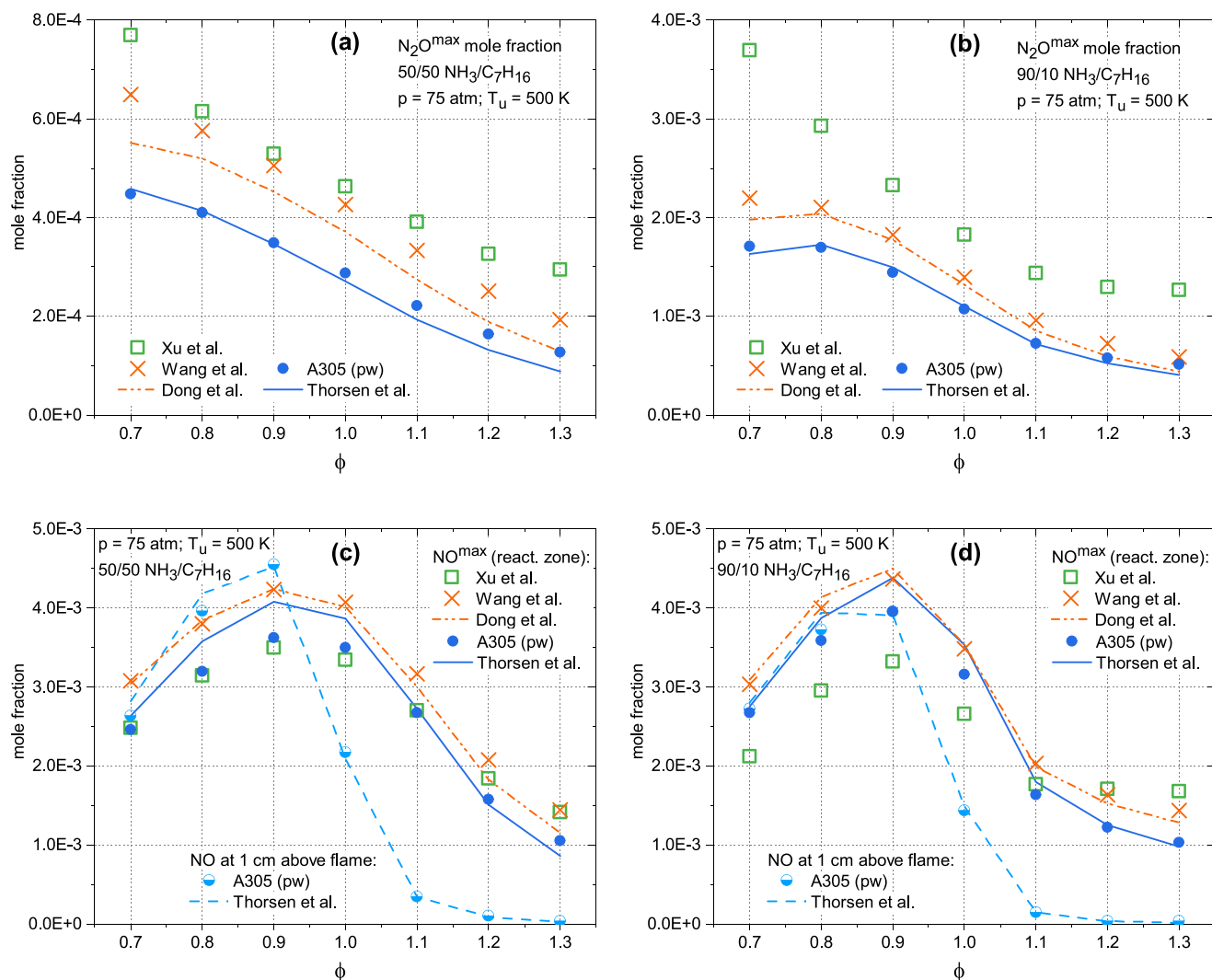
When reverted, the rate constant [58] becomes practically identical to Klippenstein and Glarborg inside the considered temperature window. For the H<sub>2</sub>NO channel, Dong et al. follow Stagni et al. [58] who use recommendations of Baulch et al. [59]. However, Baulch et al. [59] provided value for the *total* rate constant of NH<sub>2</sub> + HO<sub>2</sub>, which at that time was believed to have H<sub>2</sub>NO + OH as the dominant channel. So, when two channels in Stagni et al. are added together, the total rate becomes twice as high as recommended by Baulch et al. Finally, Bertolino et al. optimized Stagni et al. mechanism, and the H<sub>2</sub>NO channel has received even higher rate (by a factor of 1.5). Fig. S5 in the SM illustrates differences in the rate constants for (R13, R14).

When Klippenstein and Glarborg [57] values are substituted into the mechanisms of Dong et al. and Bertolino et al., the predictions of all mechanisms for the conditions of Fig. 8a become much closer to each other (see Fig. S5 in the SM). Discrepancies at other pressures and temperatures still exist, however, the purpose of this subsection is not to perform an analysis of the detailed mechanisms (which is outside the scope of this work), but to highlight that selection of the detailed mechanism as a reduction target is an important step before reduction process.

### 3.3. Effect of CO on N<sub>2</sub>O formation

In the modeling of the previous subsection, it was assumed that diluent gas consists of N<sub>2</sub> with presence of NO. The real product gas of NH<sub>3</sub>/n-heptane combustion, however, will also contain CO<sub>2</sub>, H<sub>2</sub>O, H<sub>2</sub> and CO. While the main products CO<sub>2</sub> and H<sub>2</sub>O can be assumed to have only a thermal effect in the considered target space, it is known that CO affects DeNO<sub>x</sub> NH<sub>3</sub> oxidation, and this has been subject of numerous studies, as listed in, e.g., [60]. Below, effect of CO on N<sub>2</sub>O formation was analyzed in the same target space as in Section 3.2.3, with a constant 1 % CO added to every NH<sub>3</sub>/O<sub>2</sub>/N<sub>2</sub>/NO mixture.

As discussed in Section 2.4, recent literature on (R2) suggests that the value implemented in the target model [37] is most likely incorrect. Its



**Fig. 7.** Maximal (reaction zone) mole fractions of  $N_2O$  (top) and  $NO$  (bottom) for two  $NH_3/n$ -heptane mixtures with 50/50 (left) and 90/10 (right) composition at  $T = 500$  K and 75 atm.; calculated with the present mechanism (dark-blue circles) and its target [37] (solid lines); Wang et al. [32] (crosses) and its target [42] (dash-dot lines), and Xu et al. [31] (squares). Also shown are  $NO$  at 10 mm above the flame front for present mechanism (light-blue circles) and its target [37] (dashed lines). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

effect on  $DeNO_x$   $N_2O$  formation is illustrated in Fig. 9. Two cases are shown here, that correspond to the same conditions as Fig. 8a,d, but with additional 1 % CO. Fig. S14 in the SM covers the complete target space. In the right panel of Fig. 9, temporal  $N_2O$  profiles for the two mixtures are shown at a single  $T = 1150$  K.

For the less diluted mixture, original rate of (R2) in [37] results in increased  $N_2O$  consumption after ca. 0.01 s (dashed blue curve in Fig. 9b), while implementation of the “slow” rate from [51] (adopted in present work) makes  $N_2O$  profile calculated with either reduced or detailed mechanism [37] comparable to a case without CO (dotted blue lines in Fig. 9a,b). Overall, end concentrations of  $N_2O$  are drastically different for all mixtures due to (R2), and literature mechanisms, either target mechanism for this work [37] or reduced model of Wang et al. [32], significantly overpredict  $N_2O$  consumption by CO.

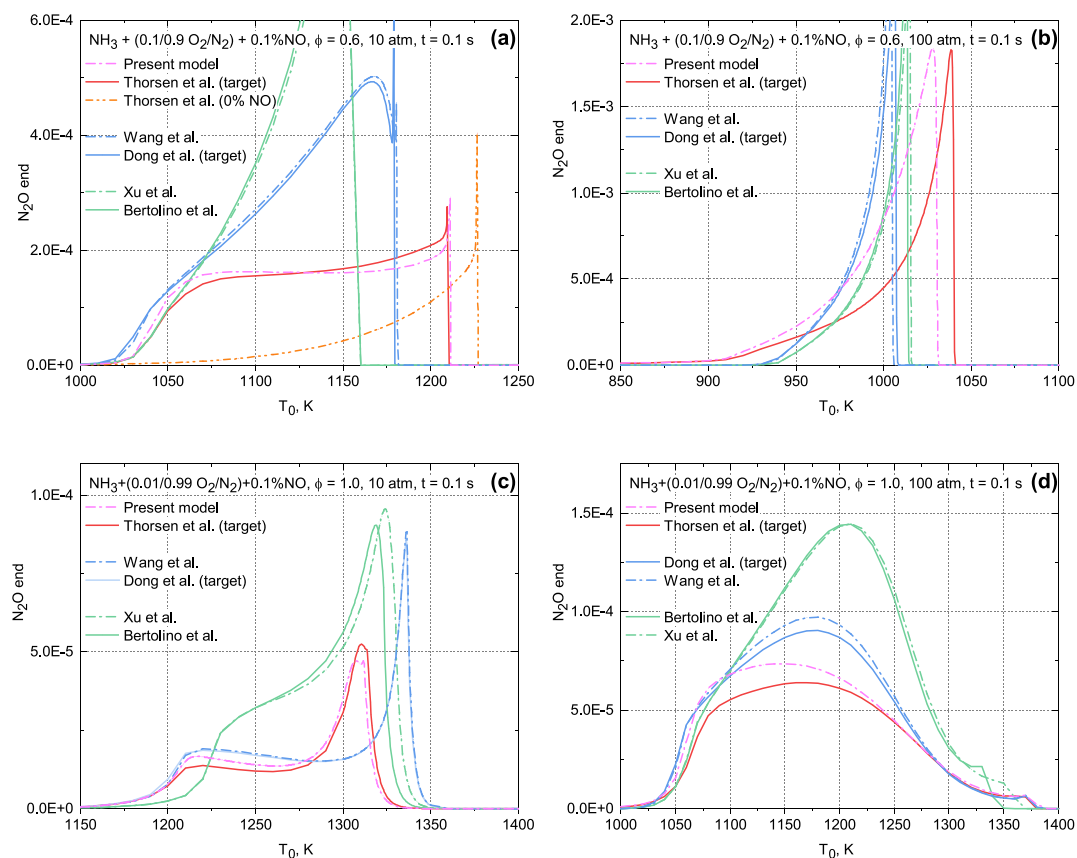
The chemical effect of CO, however, is not only limited to the speed of (R2). This is best seen for the more diluted mixture (Fig. 9c,d) by comparing the predictions of Thorsen et al. [37] with “slow” (R2) (solid blue) and the “inert-CO” curve (dot blue). CO chemically hinders  $N_2O$  formation at the initial stage (see Fig. 9d), resulting in qualitatively different  $N_2O$  profiles. Reaction analysis has identified that a major contributing reaction is  $CO + NO_2 = CO_2 + NO$  (R7) that consumes  $NO_2$ , needed for  $N_2O$  formation via (R12). This is also illustrated by

comparing predictions of the reduced mechanism with (solid red) and without (dotted red) (R7). Some disagreement still exists between the present mechanism (solid red) and [37] with “slow” (R2) (solid blue), however, addition of extra species, e.g.,  $HNCO$  and  $NCO$ , was found to be necessary for improvement, which was considered impractical. In addition to oxidation, some differences due to (R2) were observed in the predicted  $N_2O$  profiles before ignition of  $NH_3/n$ -heptane mixtures (see Fig. S15 in SM).

In this subsection two things were highlighted. First, available detailed and reduced models might underpredict  $N_2O$  concentrations if mixtures containing CO are considered. Second, even though the effect of CO might not be as dramatic as literature models predict, it might still be insufficient to completely omit all chemical interactions between nitrogen-containing species and CO in the reduced models.

#### 4. Conclusions

A new reduced mechanism is developed for use in simulations of  $NH_3$  combustion in dual-fuel IC engines. The target space for reduction (see Table 2) has been identified after a review of experimental studies of  $NH_3$  engines, to the authors knowledge including all published work on this topic up until mid 2023. Diesel was found to be the most common



**Fig. 8.**  $\text{N}_2\text{O}$  end concentrations (at 0.1 s) vs. initial temperature for mixtures of 10.5/90.5  $\text{O}_2/\text{N}_2$  ratio with  $\phi = 0.6$  (top), and 1/99  $\text{O}_2/\text{N}_2$  with  $\phi = 1.0$  (bottom). Pressures are 10 atm (left) and 100 atm (right). Solid lines: detailed (target) mechanisms, dash-dot: reduced mechanisms, dash-dot-dot: no initial presence of NO.

secondary component of the dual fuel, which was approximated by n-heptane in the present work. The considered space for reduction included 626 combustion cases that covered ignition, flames and oxidation of  $\text{NH}_3/\text{n-heptane}$  mixtures, and they were simulated in real time during reduction. Particularly, mixtures with very low molar percentage of n-heptane were considered, which have been observed to have a distinct ignition behavior and are very important for the applications since the pilot fuel is expected to be included in small proportion. Emission of  $\text{N}_2\text{O}$ , a strong greenhouse gas, was also targeted. The modeled combustion and oxidation cases were constructed with the goal to preserve the ability of the mechanism to capture formation of  $\text{N}_2\text{O}$  via two possible routes advocated for in the experimental studies, i.e., the disrupted flame mechanism and the DeNOx mechanism, occurring when unburned  $\text{NH}_3$  reacts with NO in product gas.

A recently published detailed mechanism [37] has served as target for reduction, and a semi-detailed base mechanism with subsets from [32,46] was constructed prior to reduction. The ant-colony reduction methodology [33] has been utilized, combined with differential evolution optimization [33] and a sequence of manual steps. The resulting reduced mechanism contains 57 species and 159 reactions (146 reversible and 13 irreversible) and is smaller than  $\text{NH}_3/\text{n-heptane}$  mechanisms available in literature, especially in terms of reactions. However, it was found that in the considered target space the present mechanism performs as good as the larger models.

The applicability range of the mechanism corresponds to the conditions listed in Table 2, e.g. range of pressures 10–100 atm, 0–100 %  $\text{NH}_3$  in the fuel mixture. The mechanism is supposed to be used under these conditions.

The present analysis show that inclusion of interaction reactions between carbon- and nitrogen-containing species is necessary for adequate reproduction of combustion of mixtures of  $\text{NH}_3$  and n-heptane.

At the same time, it was found to be possible to remove all reaction chain involving species containing both carbon and nitrogen atoms.

It has been observed that differences in predictions between  $\text{NH}_3/\text{n-heptane}$  reduced mechanisms are often caused by selection of rate constants of key reactions in the corresponding detailed mechanisms, highlighting the importance of relying on recent data for these rate constants.

Following the analysis of the influence of CO on  $\text{N}_2\text{O}$  formation during oxidation of  $\text{NH}_3$  in presence of NO, performed in the present work, one reaction rate (R2) in [37], which significantly affected the results, has been replaced. This has been done by revisiting available data on the rate constant of (R2). It has been concluded that CO might have an effect on post-flame  $\text{N}_2\text{O}$  consumption, however, it is not as large as predicted by available models.

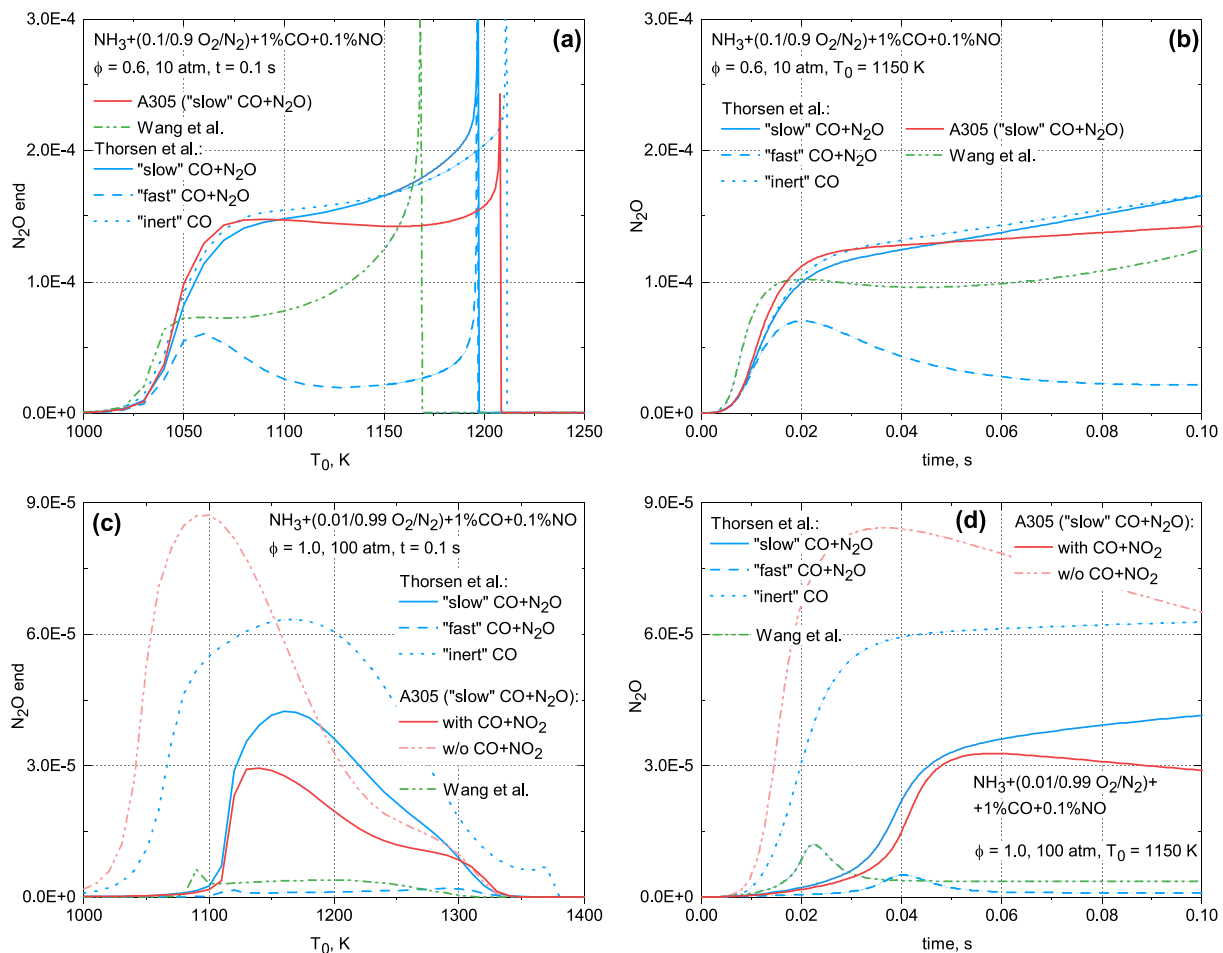
The results have indicated that post-flame oxidation of  $\text{NH}_3$  might play a role in formation of  $\text{N}_2\text{O}$ . For that reason, if these effects are to be captured in CFD simulations of  $\text{NH}_3$  engines, the implemented simulation approach has to consider occurrence of chemical reactions outside flame areas.

#### CRediT authorship contribution statement

**Vladimir A. Alekseev:** Writing – original draft, Visualization, Validation, Methodology, Investigation, Formal analysis, Conceptualization. **Elna J.K. Nilsson:** Writing – review & editing, Supervision, Project administration, Methodology, Funding acquisition, Conceptualization.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence



**Fig. 9.**  $\text{N}_2\text{O}$  end concentrations (at 0.1 s) vs. initial temperature (left), and temporal  $\text{N}_2\text{O}$  profiles at  $T = 1150$  K (right) for two initial mixtures of Fig. 8a (top) and Fig. 8d (bottom) with additional 1 % CO (by mole). The present mechanism A305 (solid red) is compared to its target [37] with a modified “slow” (R26) (solid blue). Also shown are: A305 w/o (R7) (dash-dot red), unmodified [37] (dashed blue), [37] with chemically inert CO (dot blue), and Wang et al. [32]. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

the work reported in this paper.

## Data availability

No data was used for the research described in the article.

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## Appendix A. Supplementary material

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.fuel.2024.131464>.

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